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LECTURE NOTES ON
STATISTICAL DECISION THEORY

I

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Lecture notes provide basic introduction to Statistical Decision Theory on the following themes: Linear Programming, Elements of Game Theory, and Optimal Statistical Decisions.

Notes are intended for students that study Statistical Decision Theory and anyone who wants to acquaint themselves with the subject.

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